## K. J. SOMAIYA INSTITUTE OF MANAGEMENT STUDIES AND RESEARCH,

 Vidyavihar, Mumbai- 400077Program: MCA I Sem- Batch (2019-22),
Subject: Mathematical and Statistical Foundation in Computer Science (End term exam)

Maximum Marks: 50
Duration: 3hrs. Date: 2 ${ }^{\text {nd }}$ December, 2019

## Instructions

1. Exam will be conducted in the Computer Lab. Use Excel where required.
2. Attempt any five questions.
3. Figures to the right indicate marks to the question.
4. Every question carry equal marks.

## QUESTION 1

5) 

(a) Determine whether the relation R on a set A is reflexive, irreflexive, symmetric, asymmetric, antisymmetric or transitive.
I. $\quad \mathrm{A}=$ set of all positive integers, aRb iff $|\mathrm{a}-\mathrm{b}| \leq 2$
(b) Let $\mathrm{B}=\{1,2,3,6,12,18\}$ and R be defined by xRy iff $\mathrm{x} / \mathrm{y}$.
I. Draw the digraph and Hasse diagram of R.
II. Determine the minimal and maximal elements.

QUESTION 2
5)
(a) Use brack tracking method to find the solution of the recurrence relation.

$$
a_{n}=2 a_{n-1}+1, b 1=7
$$

(b) What is the homogeneous solution of the following recurrence relation $a_{n}=a_{n-1}+2 a_{n-2}$ with the initial conditions $a_{0}=2, a_{1}=7$.

## QUESTION 3

(5+5)
(a) Let $\mathrm{S}=\{1,2,3,4\}$ and let $\mathrm{A}=\mathrm{SxS}$. Define the following relation R on A :
$(a, b) R\left(a^{\prime}, b^{\prime}\right)$ iff $a+b=a^{\prime}+b^{\prime}$
I. Show that R is an equivalence relation.
II. Compute $\mathrm{A} / \mathrm{R}$
(b) Find the value of the mean, median and mode from the data given below:

| No of <br> days <br> absent | Less <br> than 5 | Less <br> than 10 | Less <br> than 15 | Less <br> than 20 | Less <br> than 25 | Less <br> than 30 | Less <br> than 35 | Less <br> than 40 | Less <br> than <br> 45 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No of <br> students | 29 | 224 | 465 | 582 | 634 | 644 | 650 | 653 | 655 |

## QUESTION 4

(5+5)
(a) The following table gives the ages and blood pressure of 10 women. Calculate the coefficient of correlation and interpreat.

| Age(X) | 56 | 42 | 36 | 47 | 49 | 42 | 60 | 72 | 63 | 55 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Blood <br> Pressure <br> (Y) | 147 | 125 | 118 | 128 | 145 | 140 | 155 | 160 | 149 | 150 |

(b) Indicate the type of scale (nominal, ordinal, interval or ratio) that is being used in each of the following questions:
I. How large is the market size for shampoos?
II. In which of the following functional areas of management do you wish to specialize in the second year?
i) Marketing
ii) Finance
iii) HR
iv) IT
III. State the order of your preference for the following colors?
i) Grey
ii) White
iii) Blue
iv) Black
IV. Was the research methods course difficult to understand:
i) $\quad \mathrm{Yes}$
ii) No
V. In which month were you born?

## QUESTION 5

(5+5)
(a ) The following is the age distribution of 125 persons. Find the coefficient of variation.

| Age | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No of <br> persons | 15 | 15 | 23 | 22 | 25 | 10 | 5 | 10 |

(b) Calculate the First and Third Quartile.

| Marks | $0-20$ | $20-40$ | $40-60$ | $60-80$ | $80-100$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| No of <br> students | 17 | 28 | 32 | 24 | 19 |

## QUESTION 6

5) 

(a) Find the Particular solution of the following recurrence relation

$$
a_{n}+5 a_{n-1}+6 a_{n-2}=42 x 4^{n}
$$

(b) Find the partial order relation, represented by the following Hasse Diagram.

G $\quad \mathrm{H}$
F
D

C
A
B

Find the following:
I. Maximal and Minimal elements
II. Greatest and least Minimal elements if they exist
III. For $\mathrm{S}=\{\mathrm{c}, \mathrm{d}, \mathrm{e}\}$, find Upper bounds, lower bounds, Least Upper Bound, and Greatest Upper Bound.

