## University of Mumbai

Examination June 2021
Examinations Commencing from 1 June 2021
Program：Computer Engineering
Curriculum Scheme：Rev2019
Examination：SE Semester IV
Course Code：CSC402 and Course Name：Analysis of Algorithm
Time： 2 hour
Max．Marks： 80
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| Q1． | Choose the correct option for following questions．All the Questions are compulsory and carry equal marks |
| :---: | :---: |
| 1. | Which of the following is not $\mathrm{O}\left(\mathrm{n}^{2}\right)$ ？ |
| Option A： | $\left(5^{10}\right) * n+990$ |
| Option B： | $\mathrm{N}^{1.45}$ |
| Option C： | $\mathrm{n}^{3} /(\sqrt{n})$ |
| Option D： | $\left(3^{50}\right) * \mathrm{n}$ |
| 2. | If A is asymptotically less efficient than B，it means？ |
| Option A： | B will be a better choice for all inputs |
| Option B： | B will be a better choice for all inputs except possibly small inputs |
| Option C： | B will be a better choice for all inputs except possibly large inputs |
| Option D： | B will be a better choice for small inputs |
| 3. | In Quicksort algorithm，there is a procedure for finding a pivot element that splits the array into two sub－arrays，each of which contains at least Two－fifth of the elements．Let $\mathrm{T}(\mathrm{n})$ be the number of comparisons required to sort n elements． Then |
| Option A： | $\mathrm{T}(\mathrm{n})<=2 \mathrm{~T}(\mathrm{n} / 5)+\mathrm{n}$ |
| Option B： | $\mathrm{T}(\mathrm{n})<=\mathrm{T}(2 \mathrm{n} / 5)+\mathrm{T}(3 \mathrm{n} / 5)+\mathrm{n}$ |
| Option C： | $\mathrm{T}(\mathrm{n})<=2 \mathrm{~T}(4 \mathrm{n} / 5)+\mathrm{n}$ |
| Option D： | $\mathrm{T}(\mathrm{n})<=2 \mathrm{~T}(\mathrm{n} / 2)+\mathrm{n}$ |
| 4. | What is the result of following recurrences $\mathrm{T}(\mathrm{n})=\mathrm{aT}(\mathrm{n} / \mathrm{b})+\mathrm{n}^{\mathrm{c}}$ ？ |
| Option A： | $\mathrm{T}(\mathrm{n})=\mathrm{O}\left(\mathrm{n}^{\log _{\mathrm{b}}{ }^{\text {a }} \text { ）}}\right.$ |
| Option B： | $\mathrm{T}(\mathrm{n})=\mathrm{O}\left(\mathrm{n}^{\mathrm{c}} \log \mathrm{n}\right)$ |
| Option C： | $\mathrm{T}(\mathrm{n})=\mathrm{O}(\mathrm{f}(\mathrm{n})$ ） |
| Option D： | $\mathrm{T}(\mathrm{n})=\mathrm{O}\left(\mathrm{n}^{2}\right)$ |
| 5. | The class of decision problems that can be solved by non－deterministic polynomial algorithms are called as． |
| Option A： | NP |
| Option B： | P |
| Option C： | Hard |
| Option D： | Complete |
| 6. | If you are sorting in ascending order with insertion sort，average case running time it will take is？ |
| Option A： | $\mathrm{O}(\mathrm{N})$ |


| Option B: | $\mathrm{O}(\mathrm{N} \log \mathrm{N})$ |
| :---: | :---: |
| Option C: | $\mathrm{O}(\log \mathrm{N})$ |
| Option D: | $\mathrm{O}\left(\mathrm{N}^{2}\right)$ |
| 7. | Worst case time complexity of merge sort is |
| Option A: | $\mathrm{O}(\mathrm{n} \log \mathrm{n})$ |
| Option B: | $\mathrm{O}\left(\mathrm{n}^{2}\right)$ |
| Option C: | $\mathrm{O}\left(\mathrm{n}^{2} \log \mathrm{n}\right)$ |
| Option D: | $\mathrm{O}\left(\mathrm{n} \log \mathrm{n}^{2}\right)$ |
| 8. | Apply Quick sort on a given sequence 61013583211 . What is the sequence after first phase, pivot is first element? |
| Option A: | 53261081311 |
| Option B: | 52368131011 |
| Option C: | 65131083211 |
| Option D: | 65328131011 |
| 9. | Consider the graph M with 3 vertices. Its adjacency matrix is shown below. Which of the following is true? |
| Option A: | Graph M has no minimum spanning tree |
| Option B: | Graph M has a unique minimum spanning trees of cost 4 |
| Option C: | Graph M has 3 distinct minimum spanning trees, each of cost 4 |
| Option D: | Graph M has 3 spanning trees of different costs |
| 10. | Given items as $\{$ value, weight $\}$ pairs $\{\{60,10\},\{20,10\},\{40,5\}\}$. The capacity of knapsack=20. Find the maximum value output assuming items to be divisible. |
| Option A: | 110 |
| Option B: | 80 |
| Option C: | 100 |
| Option D: | 40 |
| 11. | A graph with negative weight cycle is having _____ no. of shortest paths |
| Option A: | One |
| Option B: | Two |
| Option C: | Zero |
| Option D: | Infinite |
|  |  |
| 12. | Floyd Warshall Algorithm falls into |
| Option A: | Greedy technique |
| Option B: | Dynamic Programming |
| Option C: | Linear Programming |
| Option D: | Backtracking |
|  |  |
| 13. | In assembly line scheduling problem, ___ lookup tables are required. |
| Option A: | 0 |
| Option B: | 1 |
| Option C: | 2 |
| Option D: | 3 |


| 14. | A travelling salesman problem with 55 cities has $\qquad$ no. of feasible tours. |
| :---: | :---: |
| Option A: | 37 arcs |
| Option B: | 54 arcs |
| Option C: | 55 arcs |
| Option D: | 990 arcs |
| 15. | is not a branch and bound strategy to generate branches |
| Option A: | LIFO branch and bound |
| Option B: | FIFO branch and bound |
| Option C: | Lowest cost branch and bound |
| Option D: | Highest cost branch and bound |
| 16. | Of the following given options, which one of the following is a correct option that provides an optimal solution for 4 -queens problem? |
| Option A: | (3,1,4,2) |
| Option B: | (2,3,1,4) |
| Option C: | $(4,3,2,1)$ |
| Option D: | (4,2,3,1) |
| 17. | Chromatic number of a graph is $\qquad$ no of colors required to color the vertices in graph. |
| Option A: | Maximum |
| Option B: | Same |
| Option C: | Minimum |
| Option D: | More than Number of vertices |
| 18. | In Rabin and Karp Algorithm, preprocessing can be done in |
| Option A: | $\theta\left(\mathrm{m}^{2}\right)$ |
| Option B: | $\theta$ (mlogn) |
| Option C: | $\theta$ (m) |
| Option D: | $\mathrm{O}(\mathrm{n})$ |
| 19. | What happens when the modulo value(q) is taken large? |
| Option A: | Complexity increases |
| Option B: | Spurious hits occur frequently |
| Option C: | Cost of extra checking is low |
| Option D: | Matching time increases |
| 20. | Given a pattern of length- 5 window, find the spurious hit in the given text string. <br> Pattern: 73992 <br> Modulus: 13 <br> Index: 01234567891011121314151617181920 <br> Text: 23590231415 2 67139192139 |


|  |  |
| :--- | :--- |
| Option A: | $6-10$ |
| Option B: | $12-16$ |
| Option C: | $3-7$ |
| Option D: | $13-17$ |


| Q2 | Solve any Four out of Six |
| :---: | :--- |
| A | Explain Master theorem with example |
| B marks each |  |
| C | Define P, NP, NP-Hard and NP-Complete Complexity Classes. |
| D | Discuss Complexity of Quicksort Algorithm in all cases. |
| E | Find LCS Binary Search Algorithm and Explain its complexity |
| F | Write short note on Rabin Karp "ABSDG" and Y= "GBSTR" |


| Q3. | Solve any Two Questions out of Three 10 marks each |
| :---: | :---: |
| A | Apply Dijkstra algorithm on following graph. Show all intermediate steps. |
| B | Explain 15 Puzzle problem with Branch and Bound method |
| C | Find a minimum cost path from A to L in the following multistage graph |

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| Question <br> Number | Correct Option <br> Enter either 'A' or ' $\mathbf{B}$ <br> or ' ' $\mathbf{'}^{\prime}$ or ' $\mathbf{D}$ '' |
| :---: | :---: |
| Q1. | C |
| Q2. | B |
| Q3. | B |
| Q4 | A |
| Q5 | A |
| Q6 | D |
| Q7 | A |
| Q8. | B |
| Q9. | C |
| Q10. | A |
| Q11. | C |
| Q12. | B |
| Q13. | C |
| Q14. | C |
| Q15. | D |
| Q16. | A |
| Q17. | C |
| Q18. | C |
| Q19. | C |
| Q20. | A |

$\theta 2 \cdot E$

Q. 3 A.

(3)


Q. 3 B

Formard apprach.

| $d$ |  |  |
| :---: | :---: | :---: |
| $L$ | $\theta$ | - |
| $K$ | 11 | $L$ |
| $J$ | 8 | $L$ |
| $J$ | 7 | $L$ |
| $H$ | 18 | $J$ |
| $G$ | 12 | $I$ |
| $F$ | 17 | $J$ |
| $E$ | 18 | $G$ |
| $D$ | 27 | $H$ |
| $C$ | 15 | $G$ |
| $B$ | 20 | $G$ |
| $A$ | 21 | $G$ |

$$
A-C-G-I-L
$$

path eost $=21$

