

University of Mumbai
Examination 2020 under cluster 3 (Lead College: FCRIT,VASHI)

Examinations Commencing from 22nd April 2021 to 30 th April 2021

Program: First Year Engineering

Curriculum Scheme: Rev2019 C Scheme

Examination: FE Semester I

Course Code: FEC101 and Course Name: Engineering Mathematics - I

Time: 2 hour

Max. Marks: 80

Q1.	Choose the correct option for following questions. All the Questions are compulsory and carry equal marks
1.	The value of $\tanh(\log x)$, if $x = \sqrt{2}$, will be given by
Option A:	$\sqrt{2}$
Option B:	$\frac{1}{4}$
Option C:	2
Option D:	$\frac{1}{3}$
2.	If $z = e^{i\theta}$, the value of $z^6 - \frac{1}{z^6}$ will be given by
Option A:	$2i \sin 6\theta$
Option B:	$2 \sin 6\theta$
Option C:	$2 \cos 6\theta$
Option D:	$-2i \sin 6\theta$
3.	The real part of $z = \sqrt{i}$ will be given by
Option A:	1
Option B:	-1
Option C:	$\frac{1}{2}$
Option D:	$\frac{1}{\sqrt{2}}$
4.	Find x , if $5 \sinh x - \cosh x = 5$
Option A:	$x = \log 3$
Option B:	$x = e^3$
Option C:	$x = -\log 3$
Option D:	$x = -3$
5.	Roots of $x^3 - i = 0$ are
Option A:	$e^{\frac{i(2k\pi+\pi)}{6}}, k = 0,1,2$
Option B:	$e^{\frac{i(4k\pi+1)}{6}}, k = 0,1,2$
Option C:	$e^{\frac{i(4k\pi+\pi)}{6}}, k = 0,1,2$
Option D:	$e^{\frac{i(4k\pi+\pi)}{3}}, k = 0,1,2$

6.	What is the value of $\sinh^{-1}(\tan\theta)$
Option A:	$\log\left(\sec\frac{\theta}{2} + \tan\frac{\theta}{2}\right)$
Option B:	$\log(\sec\theta + \tan\theta)$
Option C:	$\log(\sec\theta)$
Option D:	$\log(\cot\theta + \tan\theta)$
7.	If $\tan(x + iy) = i$, then the value of y is
Option A:	$\log 2$
Option B:	$\frac{1}{4}\log \log 2$
Option C:	indeterminate
Option D:	∞
8.	Imaginary part of $\text{Log}(3+4i)$ is
Option A:	$\tan^{-1}\left(\frac{4}{3}\right)$
Option B:	$\log 5$
Option C:	$\tan^{-1}\left(\frac{4}{3}\right) + 2n\pi$
Option D:	$\tan^{-1}\left(\frac{4}{3}\right) + 2\pi$
9.	If PAQ is in the normal form of A, where A is a non-singular square matrix of order 3, then A^{-1} will be,
Option A:	PQ
Option B:	QP
Option C:	$Q^{-1}P^{-1}$
Option D:	$P^{-1}Q^{-1}$
10.	The rank of a Unitary matrix of order n is
Option A:	$n - 1$
Option B:	$n + 1$
Option C:	n
Option D:	$n + 2$
11.	Find for which value of λ and μ the simultaneous equations $x+y+z=6$, $x+2y+3z=10$, $x+2y+\lambda z=\mu$ have infinite number of solution
Option A:	$\lambda = 3, \mu = 10$
Option B:	$\lambda \neq 3, \mu = 10$
Option C:	$\lambda = 3, \mu$ can take any value
Option D:	$\lambda = 3, \mu \neq 10$
12.	For which value of λ the following system of equations $3x + y - \lambda z = 0$, $4x - 2y - 3z = 0$, $2\lambda x + 4y + \lambda z = 0$ have non-trivial solution?
Option A:	$\lambda \neq -9$ and $\lambda = 1$
Option B:	$\lambda = -9$ and $\lambda = 1$
Option C:	$\lambda = -9$ and $\lambda \neq 1$
Option D:	$\lambda = 9$ and $\lambda = 1$

13.	If $u = e^{\frac{x}{y}}$, then find the value of $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2}$ is
Option A:	1
Option B:	$\frac{1}{2}$
Option C:	-1
Option D:	0
14.	If $z = f(x,y)$ and $x = uv$, $y = \frac{u}{v}$, then the value of $\frac{\partial z}{\partial u}$ will be given by
Option A:	$v \frac{\partial z}{\partial x} - \frac{1}{v} \frac{\partial z}{\partial y}$
Option B:	$\frac{\partial z}{\partial x} + \frac{\partial z}{\partial y}$
Option C:	$v \frac{\partial z}{\partial x} + \frac{1}{v} \frac{\partial z}{\partial y}$
Option D:	$v \frac{\partial z}{\partial x} + u \frac{\partial z}{\partial y}$
15.	If $z = \log \log r$, $r = x^2 + y^2$ then find the value of $x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y}$
Option A:	-2
Option B:	2
Option C:	$2r$
Option D:	$\frac{1}{r}$
16.	If $z = \frac{x}{y} + \frac{y}{x}$, then the value of $\frac{\partial^2 z}{\partial x \partial y}$ is
Option A:	$-\frac{1}{x^2} - \frac{1}{y^2}$
Option B:	$-\frac{1}{x^2}$
Option C:	$-\frac{1}{y^2}$
Option D:	$\frac{1}{x^2} + \frac{1}{y^2}$
17.	If $y = \sin^2 x$, find y_{10}
Option A:	$-2^9 \cos 2x$
Option B:	$2^9 \cos 2x$
Option C:	$2^9 \sin 2x$
Option D:	$-2^9 \sin 2x$
18.	If $y = x^n \log x$, then y_{n+1} is
Option A:	$n! x$
Option B:	$n! \log x$
Option C:	$\frac{n!}{x}$
Option D:	$n!$
19.	If $(1 + x^2) y_2 = 1$, then choose the correct option

Option A:	$(1 + x^2)y_{n+2} + 2nx y_{n+1} + n(n - 1)y_n = 0$
Option B:	$y_{n+2} + 2nx y_{n+1} - n(n - 1)y_n = 0$
Option C:	$y_{n+2} - 2nx y_{n+1} + n(n - 1)y_n = 0$
Option D:	$y_{n+2} + 2nx y_{n+1} + n^2 y_n = 0$
20.	The stationary values for $f(x, y) = xy(3 - x - y)$ are
Option A:	$(0,0), (3,0), (1,1), (1,-1)$
Option B:	$(0,0), (0,3), (3,0), (1,1)$
Option C:	$(0,0), (0,-3), (3,3), (1,1)$
Option D:	$(0,0), (0,-3), (3,0), (1,1)$

Q2 . (20 Marks)	Solve any Four out of Six	5 marks each
A	If $\cos \cos 6\theta = a \cos^6 \theta + b \cos^4 \theta \sin^2 \theta + c \cos^2 \theta \sin^4 \theta + d \sin^6 \theta$, find a,b,c,d.	
B	If $\log \log \sin \sin (x + iy) = a + ib$, prove that i) $2e^{2a} = \cosh \cosh 2y - \cos \cos 2x$ ii) $\tan \tan b = \cot \cot x \tan \tan hy$	
C	Find the non singular matrices P and Q such that PAQ is in the normal form and hence find Rank of the following matrix $A = [2 \ 1 \ 1 \ 1 \ 0 \ 1 \ 3 \ 1 \ 2 \ 3 \ 2 \ 5]$	
D	Find a,b,c and A^{-1} if $A = [1 \ 2 \ a \ 2 \ 1 \ b \ 2 \ -2 \ c]$ is orthogonal.	
E	Divide 24 into 3 parts such that the continued product of the first, square of second and cube of the third is maximum using Lagrange's method.	
F	If $u = f(x^2 - y^2, y^2 - z^2, z^2 - x^2)$, then prove that $\frac{1}{x} \frac{\partial u}{\partial x} + \frac{1}{y} \frac{\partial u}{\partial y} + \frac{1}{z} \frac{\partial u}{\partial z} = 0$	

Q3. (20 Marks)	Solve any Four out of Six	5 marks each
A	Find the continued product of the roots of $x^4 = 1 + i$	
B	Prove that $2e^{2x} = 2v - \cos \cos 2u$, where $e^z = \sin \sin (u + iv)$ and $z = x + iy$	
C	Express the matrix $[1 + 2i \ 2 \ 3 - i \ 2 + 3i \ 2i \ 1 - 2i \ 1 + i \ 0 \ 3 + 2i]$ as $P+iQ$, where both P and Q are Hermitian.	
D	If $x = \cos \cos h \left(\frac{1}{m} \log \log y \right)$, then prove that $(x^2 - 1)y_{n+2} + (2n + 1)xy_{n+1} + (n^2 - m^2)y_n = 0$	
E	If $u = \log \log r$, and $r^2 = x^2 + y^2$, then prove that $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2} + 1 = 0$	

F

If $u = \log \log \frac{x+y}{\sqrt{x^2+y^2}} + \sin^{-1} \frac{x+y}{\sqrt{x+y}}$, prove that

$$x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2} = -\frac{\sin w \cos \cos 2w}{4 \cos^3 w},$$

where $w = \sin^{-1} \frac{x+y}{\sqrt{x+y}}$

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Curriculum Scheme: Rev2019

Examination: First Year Semester I

Course Code: _FEC101_____ and Course Name: _EM-I_____

Time: 2 hours

Max. Marks: 80

Question Number	Correct Option (Enter either 'A' or 'B' or 'C' or 'D')
Q1.	D
Q2.	A
Q3	D
Q4	A
Q5	C
Q6	B
Q7	D
Q8	C
Q9.	B
Q10.	C
Q11.	A
Q12.	B
Q13.	D
Q14.	C
Q15.	B
Q16.	A
Q17.	B
Q18.	C
Q19.	A
Q20.	B