

K. J. Somaiya Institute of Technology, Sion, Mumbai-22
(Autonomous College Affiliated to University of Mumbai)

Nov – Dec 2024-2025		
(B. Tech) Program: <u>Artificial Intelligence & Data Science</u> Scheme :- <u>JB III</u>		
Regular Examination: SY Semester: III		
Course Code: <u>AIC305</u> and Course Name: Discrete structure & Data Science		
Date of Exam: 30/11/2024	Duration: 02.5 Hours	Max. Marks: 60

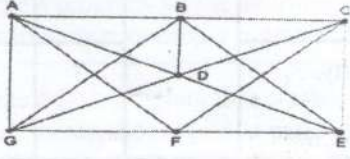
Instructions:

- (1) All questions are compulsory.
- (2) Draw neat diagrams wherever applicable.
- (3) Assume suitable data, if necessary.

Q. No.	Question	Max. Marks	CO	BT level
Q 1	Solve any two questions out of three: (05 marks each)	10		
a)	Prove $(p \wedge q)$ and $\sim p \vee \sim q$ are Logically equivalent (De Morgan's laws)		1	Ap
b)	Consider the set A {1,2,3, 4, 5} Find the cardinality of relation $R = \{ \langle x, y \rangle x, y \in A \text{ and } x \leq y \}$. Write the matrix and draw the graph which representing R.		2	Ap
c)	Consider the lattices $L_1 = \{1, 2, 4\}$, $L_2 = \{1, 3, 9\}$. Under divisibility. Draw the lattice $L_1 \times L_2$.		3	Ap
Q 2	Solve any two questions out of three: (05 marks each)	10		
a)	How many different binary numbers can be generated if the length of the number is 5 ?		4	Ap
b)	Define Monoid and it's conditions.		5	Ap
c)	Can a single graph of 8 vertices have 40 edges excluding self-loop?		6	U
Q.3	Solve any two questions out of three. (10 marks each)	20		
a)	Solve that $1^3 + 2^3 + 3^3 + \dots + n^3 = (1+2+3+\dots)^2$ by Mathematical Induction		1	Ap
b)	Solve the recurrence relation $2a_{n+2} - 11a_{n+1} + 5a_n = 0; n \geq 0, a_0 = 2, a_1 = -8$		4	An
c)	Consider the (3,5) group encoding function $e: B^3 \rightarrow B^5$ defined by $e(000)=00000$ $e(100)=10011$ $e(001)=00110$ $e(101)=10101$ $e(010)=01001$ $e(110)=11010$ $e(011)=01111$ $e(111)=11100$ Decode the following words relative to maximum likelihood decoding function. i) 11001 ii) 01010 iii) 00111.		5	Ap

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Q.4	Solve any two questions out of three. (10 marks each)	20		
a)	Let $A = \{1,2,3,4\}$ and Let $R = (1,1), (1,4), (2,2), (2,3), (3,2), (3,3), (4,1), (4,4)$. Find Transitive closure by Warshall's algorithm	2		An
b)	For the set $X = \{2,3,6,12,24,36\}$, a relation \leq is defined as $x \leq y$ if x divide y . Draw the Hasse diagram for (X, \leq) . Answer the following i) What are the maximal and minimal elements? ii) Give one example of chain and antichain Is the Poset is lattice.	3		Ap
c)	Determine the Eulerian path circuit if any, in the following graphs which is shown in fig 	6		Ap
