

K. J. Somaiya Institute of Technology, Sion, Mumbai-22
(Autonomous College Affiliated to University of Mumbai)

May-June 2025

B. Tech Program: Computer Engineering Scheme I/II/IIB/III: III

Regular: SY Semester: IV

Course Code: CEC402 and Course Name: Analysis of Algorithms

Duration: 02.5 Hours

Max. Marks: 60

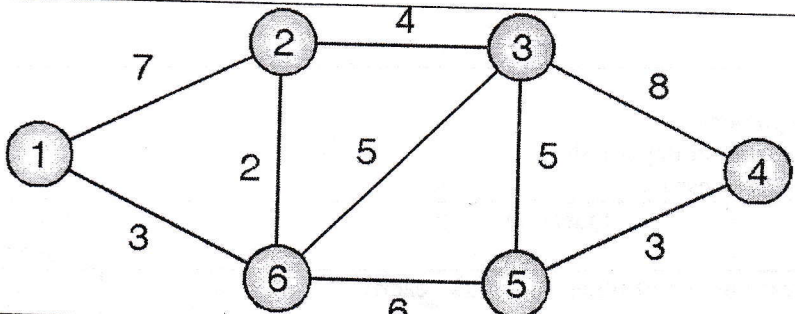
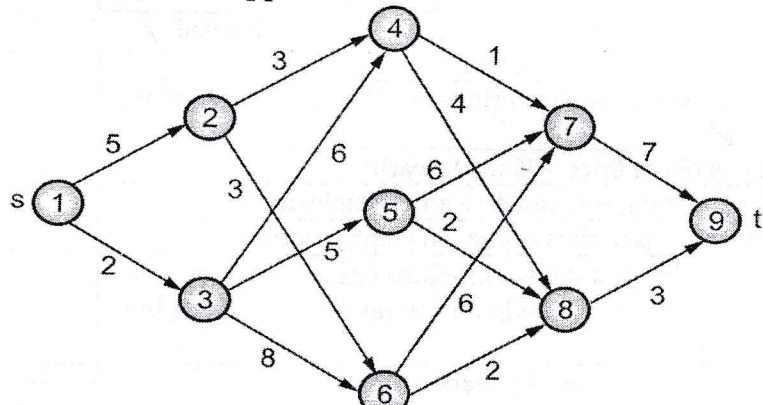
Date of Exam: 21/05/2025

Instructions:

- (1) All questions are compulsory.
- (2) Draw neat diagrams wherever applicable.
- (3) Assume suitable data, if necessary.

| (2) Draw neat diagrams with proper labels. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|--|--|------------|----------|----------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|--|---|---|-------|---|---|----------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|--|---|---|-------|---|---|-----|----|
| (3) Assume suitable data, if necessary. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q. No. | Question | Max. Marks | CO | BT level | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q 1 | Solve any two questions out of three: (05 marks each) | 10 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| a) | Solve the following recurrence relation using masters method i) $T(n) = 7T(n/2) + 18n^2$ ii) $T(n) = 9T(n/3) + 4n^6$ | | CO1 | Ap | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| b) | Apply quick sort to sort the list {E,X,A,M,P,L,E} by using divide and conquer approach using pivot as first element | | CO2 | Ap | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| c) | Compare Minimum Cost Spanning Tree Prim's and Kruskal's Algorithm (05 Points) | | CO3 | U | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q 2 | Solve any two questions out of three: (05 marks each) | 10 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| a) | Write an algorithm for selection sort and derive its complexity | | CO1 | U | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| b) | Explain how backtracking approach is applied in graph coloring problem | | CO5 | U | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| c) | Determine how many valid hits the Rabin-Karp string matcher encounters in the text $T = \text{"aaaaab"}$ when looking for the pattern $P = \text{"aab"}$ with modulo $q=13$. | | CO6 | Ap | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Q.3 | Solve any two questions out of three. (10 marks each) | 20 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| a) | Write an algorithm for Quicksort and analyze it with respect to the worst, best and average-case. | | CO2 | U | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| b) | Solve the following instance of assembly line scheduling using dynamic programming approach <div style="display: flex; justify-content: space-around; align-items: flex-start;"><div style="text-align: center;"><p>Processing Time/Assembling Time</p><table><tr><td>P_{ij}</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr><tr><td>1</td><td>7</td><td>9</td><td>3</td><td>4</td><td>8</td><td>4</td></tr><tr><td>2</td><td>8</td><td>5</td><td>6</td><td>4</td><td>5</td><td>7</td></tr></table><p>Entry Time</p><table><tr><td></td><td>1</td><td>2</td></tr><tr><td>e_i</td><td>2</td><td>4</td></tr></table></div><div style="text-align: center;"><p>Transferring time</p><table><tr><td>t_{ij}</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr><tr><td>1</td><td>2</td><td>3</td><td>1</td><td>3</td><td>4</td></tr><tr><td>2</td><td>2</td><td>1</td><td>2</td><td>2</td><td>1</td></tr></table><p>Exit Time</p><table><tr><td></td><td>1</td><td>2</td></tr><tr><td>x_i</td><td>3</td><td>2</td></tr></table></div></div> | | P_{ij} | 1 | 2 | 3 | 4 | 5 | 6 | 1 | 7 | 9 | 3 | 4 | 8 | 4 | 2 | 8 | 5 | 6 | 4 | 5 | 7 | | 1 | 2 | e_i | 2 | 4 | t_{ij} | 1 | 2 | 3 | 4 | 5 | 1 | 2 | 3 | 1 | 3 | 4 | 2 | 2 | 1 | 2 | 2 | 1 | | 1 | 2 | x_i | 3 | 2 | CO4 | Ap |
| P_{ij} | 1 | | 2 | 3 | 4 | 5 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 7 | 9 | 3 | 4 | 8 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2 | 8 | 5 | 6 | 4 | 5 | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 1 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| e_i | 2 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| t_{ij} | 1 | 2 | 3 | 4 | 5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 2 | 3 | 1 | 3 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2 | 2 | 1 | 2 | 2 | 1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 1 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| x_i | 3 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| c) | Using Dijkstra's shortest path algorithm, determine shortest path from vertex 1 for the following graph. | CO3 | Ap | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

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|---|---|----|-----|----|
|  | | | | |
| Q.4 | Solve any two questions out of three. (10 marks each) | 20 | | |
| a) | Find the minimum cost path from s to t in the following multistage graph using forward approach | 20 | CO4 | Ap |
|  | | | CO1 | Ap |
| b) | (i) Explain Big-oh, Omega and Theta Notations with the help of Graph. (05M) (ii) And represent the following function using above notations. (05M) a. $T(n) = 3n + 2$ b. $T(n) = 10n^2 + 2n + 1$ | | CO5 | Ap |
| c) | Solve the following sum of subset problem using backtracking: $n = 7$, required sum = 15, weights = [2,3,5,6,7,8,9] | | | |
