Program: Computer Engineering
Curriculum Scheme: Rev2019
Examination: MEAI Semester I
Course Code: MEAIC103 and Course Name: Mathematical Foundations of Data Science Time: 2 hour

Max. Marks: 80
$=$

| Qu-1 | Choose the correct option for following questions. All the Questions are compulsory and carry equal marks |
| :---: | :---: |
| 1. | The Central Limit Theorem says that the sampling distribution of the sample mean is approximately normal if |
| Option A: | all possible samples are selected |
| Option B: | the sample size is large |
| Option C: | the standard error of the sampling distribution is small |
| Option D: | the population size is large |
| 2. | A researcher wishes to find out about the mean of a population. She takes a sample, calculates the sample mean and works out the $95 \%$ confidence interval for the population mean. Which of the following results would she prefer? |
| Option A: | The confidence interval is very wide |
| Option B: | The confidence interval is very narrow |
| Option C: | It makes no difference to her what the width of the confidence interval is |
| Option D: | The mean is large |
|  |  |
| 3. | Parametric test, unlike the non-parametric tests, make certain assumptions about |
| Option A: | The population size |
| Option B: | The underlying distribution |
| Option C: | The sample size |
| Option D: | The data size |
|  |  |
| 4. | The sampling error is defined as? |
| Option A: | difference between population and parameter |
| Option B: | difference between sample and parameter |
| Option C: | difference between parameter and sample |
| Option D: | difference between population and sample |
|  |  |
| 5. | Two types of errors associated with hypothesis testing are Type I and Type II. Type II error is committed when |
| Option A: | We reject the null hypothesis whilst the alternative hypothesis is true |
| Option B: | We reject a null hypothesis when it is true |
| Option C: | We accept a null hypothesis when it is not true |
| Option D: | We accept a null hypothesis when it is true |
|  |  |
| 6. | The area under a standard normal curve is? |
| Option A: | 0 |


| Option B: | $\infty$ |
| :---: | :---: |
| Option C: | not defined |
| Option D: | 1 |
| 7. | Poisson distribution is applied for |
| Option A: | Continuous Random Variable |
| Option B: | Discrete Random Variable |
| Option C: | Irregular Random Variable |
| Option D: | Uncertain Random Variable |
| 8. | Consider a random variable with exponential distribution with $\lambda=1$. Compute the probability for $\mathrm{P}(\mathrm{X}>3)$. |
| Option A: | $\mathrm{e}^{-1}$ |
| Option B: | $\mathrm{e}^{-2}$ |
| Option C: | $\mathrm{e}^{-3}$ |
| Option D: | $\mathrm{e}^{-4}$ |
| 9. | An eigenvalue, corresponding to a real non zero eigenvector, points in a direction in which it is stretched by the transformation and the eigenvector is the factor by which it is stretched. |
| Option A: | True |
| Option B: | False |
| 10. | Find the rank of matrix $\left[\begin{array}{cccc} -1 & 0 & -1 & 2 \\ 2 & 0 & 2 & 0 \\ 1 & 0 & 1 & -1 \end{array}\right]$ |
| Option A: | 2 |
| Option B: | 3 |
| Option C: | 0 |
| Option D: | 4 |
| 11. | What is the principle of factorization? |
| Option A: | Every square matrix can be expressed as a product of a lower triangular matrix and upper triangular matrix |
| Option B: | Determinant of an identity matrix is one |
| Option C: | There exists no inverse for a singular matrix |
| Option D: | Every matrix can be expressed as a sum of a skew symmetric and a symmetric matrix |
|  |  |
| 12. | Which of the following is an application of the edit distance problem? |
| Option A: | Approximate string matching |
| Option B: | Spelling correction |
| Option C: | Similarity of DNA |
| Option D: | All of the mentioned |
|  |  |


| 13. | Normal Distribution is symmetric is about |
| :---: | :---: |
| Option A: | Variance |
| Option B: | Standard Deviation |
| Option C: | Mean |
| Option D: | Covariance |
|  |  |
| 14. | Covariance |
| Option A: | measures the degree to which two variables co-vary |
| Option B: | measures of the strength of relationship between two variables |
| Option C: | Dependents on the units of measurement of the variables |
| Option D: | All of the mentioned |
|  |  |
| 15. | The magnitude of the difference between observed frequencies and expected frequencies is called |
| Option A: | Chi-square value |
| Option B: | $F$ value |
| Option C: | Z value |
| Option D: | t value |
|  |  |
| 16. | Which of the following statements is false? |
| Option A: | The $t$ distribution is symmetric about zero |
| Option B: | The $t$ distribution is more spread out than the standard normal distribution |
| Option C: | As the degrees of freedom get smaller, the $t$-distribution's dispersion gets smaller |
| Option D: | The $t$ distribution is mound-shaped |
|  |  |
| 17. | A random sample of size 20 taken from a normally distributed population resulted in a sample variance of 32 . The lower limit of a $90 \%$ confidence interval for the population variance would be: |
| Option A: | 52.185 |
| Option B: | 20.170 |
| Option C: | 20.375 |
| Option D: | 54.931 |
|  |  |
| 18. | A dice is thrown twice. What is the probability of getting two numbers whose product is even? |
| Option A: | 6/4 |
| Option B: | 1/2 |
| Option C: | 3/4 |
| Option D: | 5/4 |
|  |  |
| 19. | Let $X$ and $Y$ be two independent random variables. Which one of the relations between expectation ( $E$ ), variance (Var) and covariance (Cov) given below is FALSE? |
| Option A: | $\mathrm{E}(\mathrm{XY})=\mathrm{E}(\mathrm{X}) \mathrm{E}(\mathrm{Y})$ |
| Option B: | $\operatorname{Cov}(\mathrm{X}, \mathrm{Y})=0$ |
| Option C: | $\operatorname{Var}(\mathrm{X}+\mathrm{Y})=\operatorname{Var}(\mathrm{X})+\operatorname{Var}(\mathrm{Y})$ |


| Option D: | $\mathrm{E}\left(\mathrm{X}^{2} \mathrm{Y}^{2}\right)=(\mathrm{E}(\mathrm{X}))^{2}(\mathrm{E}(\mathrm{Y}))^{2}$ |
| :---: | :--- |
|  | A sample of 15 data is as follows: $17,18,17,17,13,18,5,5,6,7,8,9,20,17,3$. <br> The mode of the data is |
| 20. | 4 |
| Option A: | 4 |
| Option B: | 13 |
| Option C: | 17 |
| Option D: | 20 |


| Qu-2 |  |
| :---: | :---: |
| A | Solve any Two 5 marks each |
| i. | Describe correlation coefficient. |
| ii. | Explain global and local optima with graphical representation. |
| iii. | Justify the need of statistics from a data science perspective. |
| B | Solve any One 10 marks each |
| i. | The average number of major storms in your city is 2 per year. What is the probability that exactly 3 storms will hit your city next year? |
| ii. | Explain Correlation matrix with example. |


| Qu-3 |  |
| :---: | :---: |
| A | Solve any Two 5 marks each |
| i. | Explain Chi-Square test. |
| ii. | Describe bootstrap permutation test in detail. |
| iii. | Explain Cosine distance with example. |
| B | Solve any One 10 marks each |
| 1. | Calculate Eigenvalue and Eigenvector for the given matrix. $\left[\begin{array}{lll} 2 & 0 & 0 \\ 0 & 3 & 4 \\ 0 & 4 & 9 \end{array}\right]$ |
| ii. | Illustrate significance of $p$ value and alpha value with example. Describe Type I and Type II error in hypothesis testing. |

## University of Mumbai

## Examination 2021 under cluster KJSIEIT

Examinations Commencing from 22 ${ }^{\text {nd }}$ April 2021 to 30 ${ }^{\text {th }}$ April 2021
Program: Computer Engineering
Curriculum Scheme: Rev2019
Examination: MEAI Semester I
Course Code: MEAIC103 and Course Name: Mathematical Foundations of Data Science
Time: 2 hour Max. Marks: 80

| Question Number | Correct Option <br> (Enter either 'A' or 'B' or 'C' or 'D') |
| :---: | :---: |
| Q1. | A |
| Q2. | B |
| Q3. | B |
| Q4 | D |
| Q5 | C |
| Q6 | D |
| Q7 | B |
| Q8. | C |
| Q9. | B |
| Q10. | A |
| Q11. | A |
| Q12. | D |
| Q13. | C |
| Q14. | D |
| Q15. | A |
| Q16. | C |
| Q17. | B |
| Q18. | C |
| Q19. | D |
| Q20. | c |

